

Max-Planck-Institut für Plasmaphysik

Physics and control of Resistive Wall Mode

Valentin Igochine

Max-Planck-Institut für Plasmaphysik, Euratom-Association, Garching, Germany





- Introduction
 - Motivation
 - •Simple dispersion relation
- Physics of the RWM
 - Electromagnetic part
 - Kinetic part
- Control of RWM
 - Control methods
 - Triggering of RWMs



Conventional tokamak scenario







Bootstrap current $|j_b \sim \nabla p|$





Figure 1. The banana current driven by the density gradient.

$$J_{\rm BS} = -\sqrt{b} \frac{RB_{\rm t}}{B_0} \left[2.44(T_{\rm e} + T_{\rm i}) \frac{{\rm d}n}{{\rm d}\psi_{\rm p}} + 0.69n \frac{{\rm d}T_{\rm e}}{{\rm d}\psi_{\rm p}} - 0.42n \frac{{\rm d}T_{\rm i}}{{\rm d}\psi_{\rm p}} \right]$$

$$j_b \sim \nabla p$$

Bootstrap current is

- in the direction of the main current
- non-inductive
- proportional to the pressure gradient











mode growth.

m=2

0.4

0.2

Mode Amplitude [a.u.]

-0.5

-1

-1.5

-2

0





RWM has global structure. This is important for "RWM \leftrightarrow plasma" interaction.

















Physics of RWMs













Mode can be represented as a surface currents

Physics: electromagnetism

Wave-particle interaction

Physics: kinetic description of the plasma-wave interaction











Simple models







Main plasma

[R. Fitzpatrick, PoP, 2002; V.D.Pustovitov, Plasma Physics Reports, 2003; A.H.Boozer, PRL, 2001]

Figure 10. 3D current pattern in vacuum vessel corresponding to the n = 0 unstable mode (the BMs are present, although not shown).

[F.Vilone, NF, 2010; E.Strumberger, PoP, 2008]



















Mode can be represented as a surface currents

Physics: electromagnetism

Physics: kinetic description of the plasma-wave interaction







Plasma rotation try to decouple RWM from the wall and plays stabilizing role

How strong the rotation stabilization? What is the critical rotation which is necessary to stabilize RWM? Is only the plasma rotation important?

The answers depend on the type of interaction between RWM and plasma rotation which is considered by the model and/or accuracy of the model for such interaction





Linearized MHD equations with influence of rotation $\rho(\gamma + in\Omega)\vec{v}_1 = -\vec{\nabla}\cdot\vec{p}_t + \vec{j}_1 \times \vec{B} + \vec{j} \times \vec{b}_1 - \vec{\nabla}\cdot\vec{\Pi}_1 - \rho\vec{U}(\vec{v}_1),$ $(\gamma + in\Omega)\vec{b}_1 = \vec{\nabla} \times (\vec{v}_1 \times \vec{B} - \eta\vec{j}_1) + (\vec{b}_1 \cdot \vec{\nabla}\Omega)R^2\vec{\nabla}\phi,$ $\vec{j}_1 = \vec{\nabla} \times \vec{b}_1,$ $(\gamma + in\Omega)p_1 = -(\vec{v}_1 \cdot \vec{\nabla})p - \Gamma p\vec{\nabla}\cdot\vec{v}_1,$ $(\gamma + in\Omega)\rho_1 = -(\vec{v}_1 \cdot \vec{\nabla})\rho - \rho\vec{\nabla}\cdot\vec{v}_1.$

Ω is the (non-uniform) rotation frequency of the plasma at equilibrium n is the toroidal mode number

In the above set of equations, $(\rho, \vec{v}, \vec{B}, \vec{j}, p_1, \vec{p_t})$ are the (density, velocity, magnetic field, current, fluid pressure and total pressure). Equilibrium quantities are denoted without suffix,





Linearized MHD equations with influence of rotation

momentum equation

$$\begin{split} \rho(\gamma + \mathrm{i}n\Omega)\vec{v}_1 &= -\vec{\nabla}\cdot\vec{p}_t + \vec{j}_1 \times \vec{B} + \vec{j} \times \vec{b}_1 - \vec{\nabla}\cdot\vec{\Pi}_1 - \rho\vec{U}(\vec{v}_1), \\ (\gamma + \mathrm{i}n\Omega)\vec{b}_1 &= \vec{\nabla} \times (\vec{v}_1 \times \vec{B} - \eta\vec{j}_1) + (\vec{b}_1 \cdot \vec{\nabla}\Omega)R^2\vec{\nabla}\phi, \\ \vec{j}_1 &= \vec{\nabla} \times \vec{b}_1, \\ (\gamma + \mathrm{i}n\Omega)p_1 &= -(\vec{v}_1 \cdot \vec{\nabla})p - \Gamma p\vec{\nabla}\cdot\vec{v}_1, \\ (\gamma + \mathrm{i}n\Omega)\rho_1 &= -(\vec{v}_1 \cdot \vec{\nabla})\rho - \rho\vec{\nabla}\cdot\vec{v}_1. \end{split}$$

Ω is the (non-uniform) rotation frequency of the plasma at equilibrium *n* is the toroidal mode number

In the above set of equations, $(\rho, \vec{v}, \vec{B}, \vec{j}, p_1, \vec{p_t})$ are the (density, velocity, magnetic field, current, fluid pressure and total pressure). Equilibrium quantities are denoted without suffix,





 $\frac{\text{Linearized MHD equations with influence of rotation}}{\rho(\gamma + in\Omega)\vec{v}_1 = -\vec{\nabla}\cdot\vec{p}_t + \vec{j}_1 \times \vec{B} + \vec{j} \times \vec{b}_1 - (\vec{\nabla}\cdot\vec{\Pi}_1 - \rho\vec{U}(\vec{v}_1), (\gamma + in\Omega)\vec{b}_1 = \vec{\nabla} \times (\vec{v}_1 \times \vec{B} - \eta\vec{j}_1) + (\vec{b}_1 \cdot \vec{\nabla}\Omega)R^2\vec{\nabla}\phi, \vec{j}_1 = \vec{\nabla} \times \vec{b}_1, (\gamma + in\Omega)p_1 = -(\vec{v}_1 \cdot \vec{\nabla})p - \Gamma p\vec{\nabla}\cdot\vec{v}_1, (\gamma + in\Omega)\rho_1 = -(\vec{v}_1 \cdot \vec{\nabla})\rho - \rho\vec{\nabla}\cdot\vec{v}_1.$

 Ω is the (non-uniform) rotation frequency of the plasma at equilibrium n is the toroidal mode number Dissipation, viscous stress tensor

One has to make approximations for kinetic description of the dissipation

In the above set of equations, $(\rho, \vec{v}, \vec{B}, \vec{j}, p_1, \vec{p}_t)$ are the (density, velocity, magnetic field, current, fluid pressure and total pressure). Equilibrium quantities are denoted without suffix,





Fluid approximation of the Landau damping:

'sound wave damping' [Hammet G W and Perkins F W 1990 Phys. Rev. Lett]

$$ec{
abla}\cdotec{\Pi}=\kappa_{||}\sqrt{\pi}|k_{||}v_{\mathrm{th}_i}|
hoec{v}_1\cdot\hat{b}\hat{b}.$$





Fluid approximation of the Landau damping:

'sound wave damping' [Hammet G W and Perkins F W 1990 Phys. Rev. Lett]

$$\vec{\nabla} \cdot \vec{\Pi} = \overbrace{\kappa_{||}}^{\mathbf{\nabla}} \sqrt{\pi} |k_{||} v_{\text{th}_{i}} |\rho \vec{v}_{1} \cdot \hat{b} \hat{b}.$$
free parameter between 0.1
and 1.5





Fluid approximation of the Landau damping:

'sound wave damping' [Hammet G W and Perkins F W 1990 Phys. Rev. Lett]

$$\vec{\nabla} \cdot \vec{\Pi} = \kappa_{||} \sqrt{\pi} |k_{||} v_{\text{th}_i}| \rho \vec{v}_1 \cdot \hat{b} \hat{b}.$$

free parameter between 0.1
and 1.5

'kinetic damping'model uses kinetic energy principle with $\omega_* = 0, \omega_D = 0$ [Bondeson A and Chu M S 1996 Phys. Plasmas]

No free parameters

magnetic drift frequency $\omega_D \sim k_\perp \rho_i v_{th}/R$, with $k_\perp \sim m/r$ diamagnetic frequency $\omega *$



Comparison of the critical rotation with experiments



Figure 14. MARS calculation of the critical plasma rotation at q = 2 for the marginal n = 1 RWM using the actual DIII-D equilibrium and wall. Data and fits are versus $\beta_N/2.4\ell_i \equiv \kappa + 1$ as in figure 11. MARS calculations are with sound wave damping model using $\kappa_{\parallel} = 0.1, 0.25$ or 0.5 or with kinetic damping model.

[LaHaye, NF, 2004]



Comparison of the critical rotation with experiments



Figure 14. MARS calculation of the critical plasma rotation at q = 2 for the marginal n = 1 RWM using the actual DIII-D equilibrium and wall. Data and fits are versus $\beta_N/2.4\ell_i \equiv \kappa + 1$ as in figure 11. MARS calculations are with sound wave damping model using $\kappa_{\parallel} = 0.1, 0.25$ or 0.5 or with kinetic damping model.

[LaHaye, NF, 2004]

BINP/ March 2016 / Lecture for Ph.D. Students

these experiments due to NBI

26





[Strait, PoP, 2007]

ΡΡ





BINP/ March 2016 / Lecture for Ph.D. Students

ΡΡ





μμ





<u>Self-consistent modeling</u> (MARS,...)

Linear MHD + approximation for damping term

• (+) rotation influence on the mode eigenfunction

• (-) damping model is an approximation

Perturbative approach (Hagis,...)

Fixed linear MHD eigenfunctions as an input for a kinetic code

• (-) rotation does not influence on the mode eigenfunctions

• (+) damping is correctly described in kinetic code





<u>Self-consistent modeling</u> (MARS,...)

Linear MHD + approximation for damping term

• (+) rotation influence on the mode eigenfunction

• (-) damping model is an approximation

Perturbative approach

<u>(Hagis,...)</u>

Fixed linear MHD eigenfunctions as an input for a kinetic code

• (-) rotation does not influence on the mode eigenfunctions

• (+) damping is correctly described in kinetic code





32





BINP/ March 2016 / Lecture for Ph.D. Students





$$\begin{split} &(\gamma + in\Omega)\xi \ = \ \mathbf{v} + (\xi \cdot \nabla\Omega) R \hat{\boldsymbol{\varphi}}, & \text{[Liu, PoP, 2008, Liu, IAEA, 2010]} \\ &\rho(\gamma + in\Omega) \mathbf{v} \ = \ -\nabla \cdot \mathbf{p} + \mathbf{j} \times \mathbf{B} + \mathbf{J} \times \mathbf{Q} - \rho \left[2\Omega \hat{\mathbf{Z}} \times \mathbf{v} + (\mathbf{v} \cdot \nabla\Omega) R \hat{\boldsymbol{\varphi}} \right] \\ &(\gamma + in\Omega) \mathbf{Q} \ = \ \nabla \times (\mathbf{v} \times \mathbf{B}) + (\mathbf{Q} \cdot \nabla\Omega) R \hat{\boldsymbol{\varphi}}, \\ &(\gamma + in\Omega) p \ = \ -\mathbf{v} \cdot \nabla P, \\ &\mathbf{j} \ = \ \nabla \times \mathbf{Q}, & \text{Kinetic effects are inside the pressure} \\ &\mathbf{p} \ = \ p \mathbf{I} + p_{\parallel} \hat{\mathbf{b}} \hat{\mathbf{b}} + p_{\perp} (\mathbf{I} - \hat{\mathbf{b}} \hat{\mathbf{b}}), \\ &p_{\parallel} e^{-i\omega t + in\varphi} = \sum_{e,i} \int d\Gamma M v_{\parallel}^2 f_L^1, & p_{\perp} e^{-i\omega t + in\varphi} = \sum_{e,i} \int d\Gamma \frac{1}{2} M v_{\perp}^2 f_L^1, \end{split}$$

• full toroidal geometry in which the kinetic integrals are evaluated

•
$$\omega_* \neq 0, \omega_D \neq 0$$





$$\begin{split} (\gamma + in\Omega)\xi &= \mathbf{v} + (\xi \cdot \nabla\Omega) R \hat{\phi}, & \text{[Liu, PoP, 2008, Liu, IAEA, 2010]} \\ \rho(\gamma + in\Omega)\mathbf{v} &= -\nabla \cdot \mathbf{p} + \mathbf{j} \times \mathbf{B} + \mathbf{J} \times \mathbf{Q} - \rho \left[2\Omega \hat{\mathbf{Z}} \times \mathbf{v} + (\mathbf{v} \cdot \nabla\Omega) R \hat{\phi} \right] \\ (\gamma + in\Omega)\mathbf{Q} &= \nabla \times (\mathbf{v} \times \mathbf{B}) + (\mathbf{Q} \cdot \nabla\Omega) R \hat{\phi}, \\ (\gamma + in\Omega)p &= -\mathbf{v} \cdot \nabla P, \\ \mathbf{j} &= \nabla \times \mathbf{Q}, & \text{Kinetic effects are inside the pressure} \\ \mathbf{p} &= p\mathbf{I} + p_{\parallel} \hat{\mathbf{b}} \hat{\mathbf{b}} + p_{\perp} (\mathbf{I} - \hat{\mathbf{b}} \hat{\mathbf{b}}), \\ p_{\parallel} e^{-i\omega t + in\phi} &= \sum_{e,i} \int d\Gamma M v_{\parallel}^2 f_L^1, \qquad p_{\perp} e^{-i\omega t + in\phi} = \sum_{e,i} \int d\Gamma \frac{1}{2} M v_{\perp}^2 f_L^1, \end{split}$$

- full toroidal geometry in which the kinetic integrals are evaluated
- $\omega_* \neq 0, \omega_D \neq 0$

...but still some strong assumptions are made: neglects the perturbed electrostatic potential, zero banana width for trapped particles, no FLR corrections to the particle orbits. There is no guaranty that all important effects are inside.





RWM is stable at low plasma rotation up to $C_{\beta} \leq 0.4$ without feedback due to mode resonance with the precession drifts of trapped particles.





RWM is stable at low plasma rotation up to $C_{\beta} \leq 0.4$ without feedback due to mode resonance with the precession drifts of trapped particles.

... but some important factors are missing (for example alpha particles are not taken into account).



Influence of α -particles on RWM in ITER (perturbative)

IPP







Control of RWMs



DIII-D: two coil sets 6 C-coils, 12 I-coils usually connected in quartets.

ASDEX Upgrade

μ



Table 3. Feedback logic and flux and method used for stabilization.

Logic	Type of flux and method of utilization
Smart shell	Uses total radial flux just outside or inside the wall:
	feedback tries to produce 'pseudo-ideal wall' at the
	observation location [32].
Fake rotating	Uses radial flux: the feedback currents are toroidally
shell	shifted relative to the observed mode pattern imitating
	the phase shift induced by toroidal rotation [58].
Explicit mode	Uses the radial flux compensated by the flux due to direct
	coupling between the coil and the sensors [144].
Mode control	Uses poloidal flux that is due to the unstable RWM and
	optimally decoupled from the applied B_r field from the
	feedback coils [86].
	M S Chu ¹ and M Okabayashi ²

Plasma Phys. Control. Fusion 52 (2010) 123001





□ Looking more closely at feedback control system components

- Sensors and mode identification
- Control logic: intelligent shell-like or including plasma response? ...
- Power supply
- Coil geometry, number and position

There are multiple possibilities in each of the points and one has to find optimum solution.



How important low n control close to the pressure limit?



43

IPP

Why the RFPs are important for RWM study?



RFX-mod control system is made by 192 active saddle coils, each independently fed. 100% coverage of the plasma surface.



RFX-mod "quantum" for active control: $\Delta \phi = 7.5^{\circ}$; $\Delta \theta = 90^{\circ}$. Area covered=0.52% RFX-mod control system is routinely working on discharges with 30-40 MW Ohmic input power, where effective control is essential.





The main idea is to test on the same plasma and on the same device different active control configurations.



NB: it is a software reconfiguration, active on selected harmonics only!

This will allow to understand how much coils we need for RWM stabilization.











From intelligent shell (SISO) to real time DFT and to dithering.



E. Olofsson et al, "Closed loop direct parametric identification of magnetohydrodynamic normal modes spectra in EXTRAP T2R reversed-field pinch," Proceedings of the 3rd IEEE Multi-conference on Systems and Control (MSC) July 2009

E. Olofsson et al, RFX-mod programme workshop, 2011







(a)Cylindrical ideal MHD resistive shell modes in theory; as seen through the discrete sensor array of T2R.

Experimental picture



(b)Growth-rate and spatial spectrum of eigenvectors of the autodetected empirical *A*-matrix.

E. Olofsson et al, Plasma Physics and Controlled Fusion (53), (084003)



Difference between current driven and pressure driven RWMs





Interaction of <u>RWM with plasma</u> is different for current driven and pressure driven RWMs. One has to investigate pressure driven cases. RFPs expertise is not applicable here.





It is important that RWM could be triggered by core (off axis fishbones) and edge (ELMs) modes. This also shows global structure of RWM. Integrated control of different MHD modes is required to stabilize RWM.



PLASMA PHYSICS AND CONTROLLED FUSION

doi:10.1088/0741-3335/52/12/123001



IOP PUBLISHING

Plasma Phys. Control. Fusion 52 (2010) 123001 (102pp)

TOPICAL REVIEW

Stabilization of the external kink and the resistive wall mode

 ${\bf M}~{\bf S}~{\bf Chu}^1$ and ${\bf M}~{\bf Okabayashi}^2$

IOP PUBLISHING and INTERNATIONAL ATOMIC ENERGY AGENCY

Nucl. Fusion 52 (2012) 074010 (13pp)

NUCLEAR FUSION

doi:10.1088/0029-5515/52/7/074010

2) Springer

pringer Series on Atomic, Optical, and Planna Physics

Valentin loochine Editor

Active Control

Instabilities in

Hot Plasmas

of Magnetohydrodynamic

SPECIAL TOPIC

Physics of resistive wall modes

V. Igochine

MPI für Plasmaphysik, Euratom-Association, D-85748 Garching, Germany

E-mail: valentine.igochine@ipp.mpg.de





RWMs may limit our operations close to the limit.





RWM stability is affected by interactions with





RWM stability is affected by interactions with resistive wall, external fields, fast particles and plasma rotation.





RWM stability is affected by interactions with resistive wall, external fields, fast particles and plasma rotation.

Stabilization at low rotations (comparable and less to what is expected for ITER) is achieved, but self consistent modeling is still a problem.

Recent modeling shows that RWMs could be stable in ITER without external feedback well above the no wall limit because of





RWM stability is affected by interactions with with resistive wall, external fields, fast particles and plasma rotation.

Stabilization at low rotations (comparable and less to what is expected for ITER) is achieved, but self consistent modeling is still a problem.

Recent modeling shows that RWMs could be stable in ITER without external feedback well above the no wall limit because of kinetic effects.

Other modes are able to trigger RWMs at low plasma rotation: ...





RWM stability is affected by interactions with with resistive wall, external fields, fast particles and plasma rotation.

Stabilization at low rotations (comparable and less to what is expected for ITER) is achieved, but self consistent modeling is still a problem.

Recent modeling shows that RWMs could be stable in ITER without external feedback well above the no wall limit because of kinetic effects.

Other modes are able to trigger RWMs at low plasma rotation: Energetic Particle Modes, ELMs





For RWM control we need:

•





For RWM control we need:

- Sensors (magnetic coils for n=1 detection)
- Actuators (large magnetic coils which would mimic ideal wall or other actions)
- control strategies and identification tools.